

Sec 1.1

Variables

- Characteristic of an "individual"

↑
people, animals
or things

- Something that varies

Types of Variables

1) Categorical / Qualitative

- No Averages Possible
- Eye Color, Gender, Zip Code ...

2) Quantitative Variables

- Averages Possible
- Height, Age, GPA, SAT Score ...

Distribution of A Variable

Tells what values a variable takes and how often it takes these values

Categorical

Pie charts
Bar graphs } p. 9

Quantitative

Dot Plots (P. 27)
Stemplots (P. 34)
Histograms (P. 37)

Relationships Between Categorical Variables

	Student Smokes	Student Not Smokes	
Both Parents Smoke	400	1380	1780
One Parent Smokes	416	1823	2239
No Parent Smokes	188	1168	1356
	1004	4371	5375

Marginal Distribution

$$\% \text{ of students smoke} = \frac{1004}{5375} = 19\%$$

Tells you nothing
about any relationship

Relationships Between Categorical Variables

	Student Smokes	Student Not Smokes	
Both Parents Smoke	400	1380	1780
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Conditional Distribution

- a) % of students smoke when both parents smoke $= \frac{400}{1780} = 22\%$
- b) % of students smoke when neither parent smokes $= \frac{188}{1356} = 14\%$
- } Compare

Conclusions

- When both parents smoke, student smoking goes from 14% to 22%
- 8% more students smoke when both parents smoke
- When both parents smoke, student smoking increases by 57% $\left(\frac{14-22}{14}\right)$

Simpson's Paradox

- "Lurking variables" which can change/reverse a relationship
- Most likely to occur when several groups are combined into single categorical group

Ex Where should I have surgery?

	Hospital A	Hospital B
Died After Surgery	63	16
Survived Surgery	2037	784
	2100	800

Hospital A loses $63/2100 = 3\%$ of patients

Hospital B loses $16/800 = 2\%$ of patients

So you choose Hospital B for your surgery

But previous data ignored the condition of the patient:

Good Condition

	A	B
Died	6	8
Survived	594	592
	600	600

Poor Condition

	A	B
Died	57	8
Survived	1443	192
	1500	200

Hospital A only loses $6/600 = 1\%$ of patients in good condition (like you) and Hospital B loses $8/600 = 1.3\%$ so... Hospital A is actually safer for you!

Organizing A Statistical Problem

"Statistic Problems Demand Consistency"

State Question you're trying to answer

Plan Statistical techniques needed

Do Needed calculations / graphs

Conclude In context of problem

Sec 1.2

Graphs of Quantitative Variables

- 1) Dotplots (P. 27)
 - 2) Stemplots (P. 35)
 - 3) Histograms (P. 37)
- } Shape $\begin{cases} \text{Symmetric} \\ \text{Skewed} \end{cases}$
Center (Median)
Spread
Outliers?

Making Graphs

1) Title

2) Label / Scale axes

↑ Include key
for stemplots

Dotplot (P. 27)

Shape - Skewed Right

Center ≈ 3

Spread = 0 to 8 or 8

Outliers - Possibly 7 and 8

Stemplot

16 Test Scores :

9|0, 8|0, 9|6, 5|4, 8|0, 9|5, 10|0, 7|5,
8|7, 6|2, 6|5, 8|5, 9|2, 8|7, 7|4, 8|9

stem
↓
1 digit (leaf)

5	4
6	2 5
7	5 4
8	0 0 7 5 7 9
9	0 6 5 2
10	0

→

5	4
6	2 5
7	4 5
8	0 0 5 7 7 9
9	0 2 5 6
10	0

86%

↓

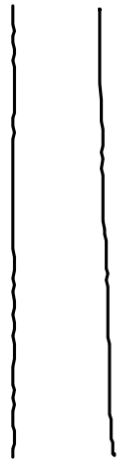
5|4
means
54%

Misc

- 1) Stems can be split (0-4, 5-9)
- 2) Use side by side stem plots to compare

Male

Female



Histograms (P. 39)

[STAT] → EDIT → [ENTER] → Data in L₁

[STATPLOT] → [ENTER] →  → [ZOOM] → [9]

↑
[2nd] → [Y=]

- Sketch ... Use [TRACE] for values

Misc

- 1) Calculator histograms use actual frequencies
- 2) Histograms using **relative frequencies** (%) need to be done by hand
- 3) Histograms are not bar graphs
- 4) When comparing data where number of observations are different, use percents (**P.40**)

Sec 1.3

Measure of Central Tendency (Center)

i) Mean (\bar{x} for samples, μ for populations)
 \uparrow "x bar" \uparrow μ

- Arithmetic average = $\frac{\sum x_i}{n}$
- Not **resistant** (affected by outliers)
- Best for symmetric distributions

2) Median (M)

- Midpoint of values

Ex 2, 4, 6 ($M = 4$)

2, 4, 6, 8 ($M = 5$)

- Very resistant

Ex 10, 20, 30 ($\bar{X} = 20$, $M = 20$)

10, 20, 100 ($\bar{X} = 43.3$, $M = 20$)

- Best for skewed distributions

Spread ☺☺☺ vs ☺ ☺ ☺

Range = max - min

Variance (s^2)

$$s^2 = \frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n-1} = \frac{1}{n-1} \sum (x_i - \bar{x})^2$$

Standard Deviation (s) = $\sqrt{\text{Variance}}$

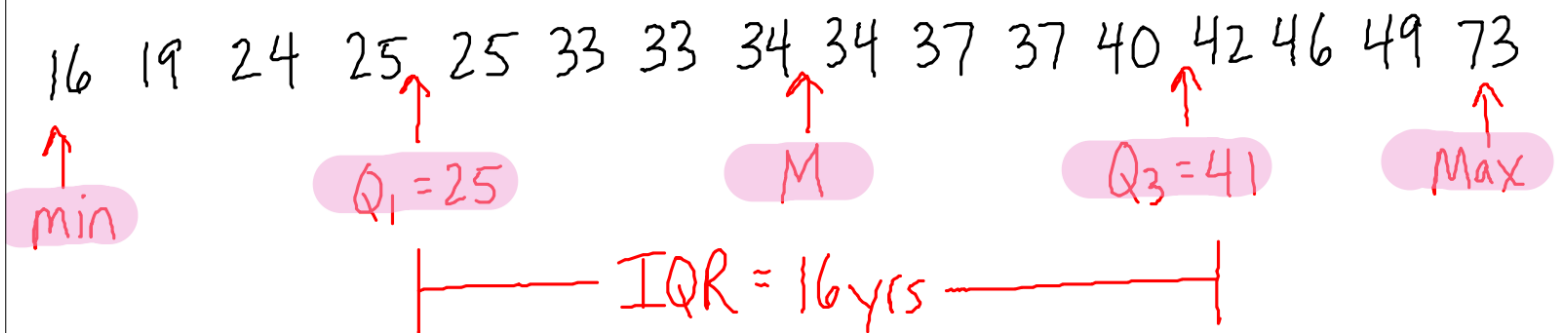
- Not resistant
- Best for symmetric distributions

Interquartile Range (IQR)

- Middle 50% = $Q_3 - Q_1$
- Best for skewed distributions

5-Number Summary + 2

Ex Ages of people at family reunion:

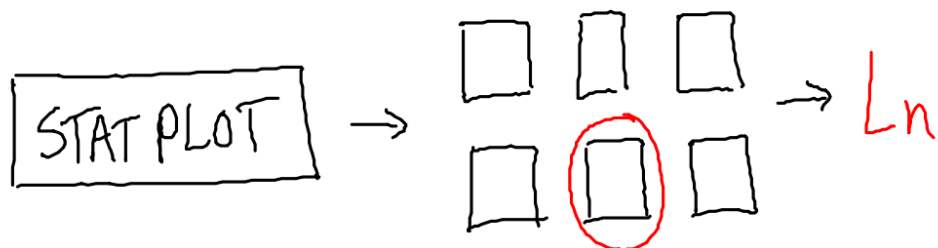
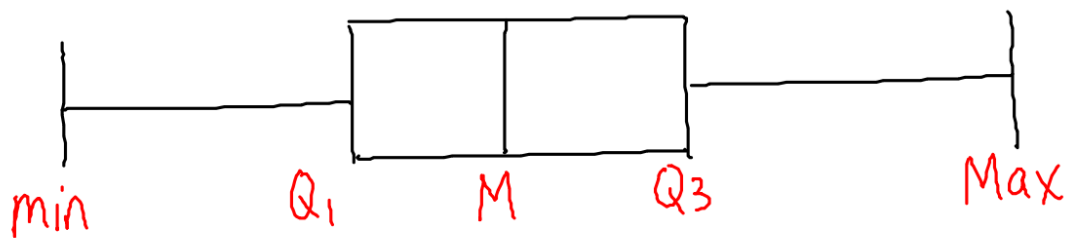


STAT → CALC → **ENTER** → 1-Var Stats Ln

$$\bar{X} = 35.44 \text{ yrs} \quad S = 13.63 \text{ yrs}$$

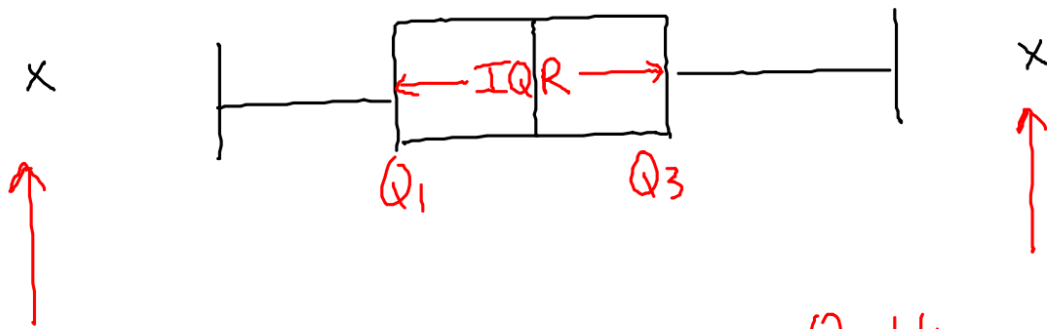
Boxplots

Used to display 5-number summary



Modified Boxplot

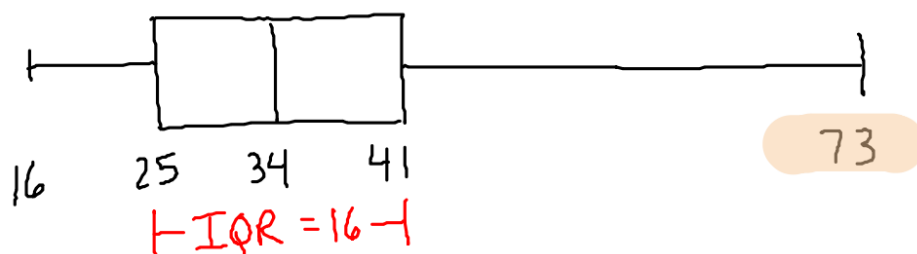
- Displays possible outliers



Outlier $< Q_1 - 1.5(IQR)$

Outlier $> Q_3 + 1.5(IQR)$

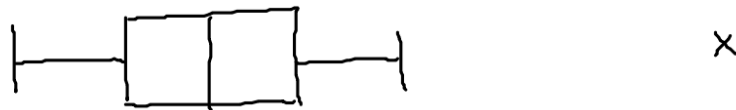
Ex Ages at family reunion



Outlier $< 25 - 1.5(16) < 25 - 24 < 1$

Outlier $> 41 + 1.5(16) > 41 + 24 > 65$

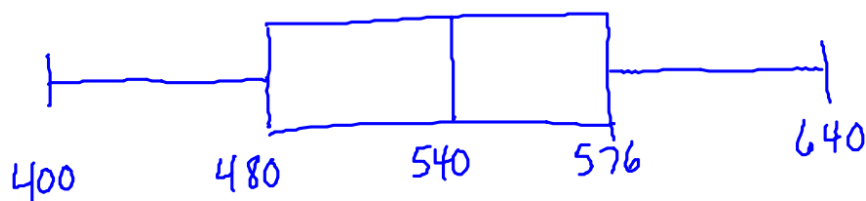
Modified Box Plot



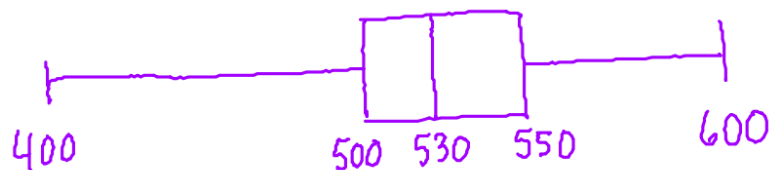
Side By Side Boxplots

L_1 = SAT Math Scores

L_2 = SAT Verbal Scores



> Plot 1



> Plot 2

Test Taking Strategies

- Review ^{Online} Notes / Homework
- Read Section Summaries (Pp 21, 42, 69)
- Practice Solving Problems
 - Practice Test
 - Chapter Review Exercises (Pp 75-78)
- Work With A Study Buddy!

↑
All answers
in back of
book!