

CHI-SQUARE GOODNESS OF FIT TEST

This test is used to determine if observed counts are equal to a hypothesized distribution.

A researcher believes the Mars Company is misleading the public on its color distribution of M&Ms. He wants to compare the color distribution from a random sample of M&Ms to the Mars Company's expected values:

	Brown	Red	Yellow	Green	Orange	Blue	Purple
Sample	4	4	16	10	8	4	4
Expected	.10 (5)	.20 (10)	.20 (10)	.10 (5)	.10 (5)	.10 (5)	.20 (10)

H STATE NULL AND ALTERNATIVE HYPOTHESES:

H₀: Color distribution of M&Ms is the same as the company claims

H_a: Color distribution of M&Ms is different than the company claims

A DETERMINE THAT CONDITIONS FOR TEST ARE ACCEPTABLE:

- Random... yes
- Every expected count ≥ 5 ...yes
- Independent... $N > 10(50) > 500$ M&Ms in population... yes

T PERFORM TEST:

a) Calculate Chi-Square statistic:

$$X^2 = \sum (O_i - E_i)^2 / E_i = (4 - 5)^2 / 5 + \dots + (4 - 10)^2 / 10 = 18.0$$

b) Determine Degrees of Freedom = Number of Categories - 1 = 7 - 1 = 6

c) Determine *P*-Value

i) Using Table C:

$$P\text{-value} < .01 \text{ for } X^2 \text{ of } 18 \text{ and degrees of freedom } 6$$

ii) Using calculator:

$$\text{DISTR} \rightarrow X^2 \text{cdf} (18, 100, 6) \rightarrow p = .006$$

S STATE CONCLUSION IN CONTEXT

There is very good evidence to reject H₀ ($p = .006$) and conclude that the color distribution of M&Ms is **not** what the company claims it should be.